

Math 103 Day 6: Derivative Rules

Ryan Blair

University of Pennsylvania

Tuesday September 28, 2010

Outline

1 Derivative Rules

Formula 1: When c is a constant

$$\frac{d}{dx}(c) = 0$$

Formula 2:

$$\frac{d}{dx}(x) = 1$$

Formula 3: When n is a positive integer,

$$\frac{d}{dx}(x^n) = nx^{n-1}$$

Formula 3: When n is a positive integer,

$$\frac{d}{dx}(x^n) = nx^{n-1}$$

fact: $(x - a)^n = (x - a)(x^{n-1} + ax^{n-2} + a^2x^{n-3} + \dots + a^{n-2}x + a^{n-1})$

Formula 4:(General Power Rule) When n is any real number,

$$\frac{d}{dx}(x^n) = nx^{n-1}$$

Formula 5: If c is a constant and f is differentiable, then

$$\frac{d}{dx}(cf(x)) = c \frac{d}{dx}(f(x))$$

Formula 6:(Sum Rule)If g and f are differentiable, then

$$\frac{d}{dx}[f(x) + g(x)] = \frac{d}{dx}[f(x)] + \frac{d}{dx}[g(x)]$$

Formula 7:(Difference Rule)If g and f are differentiable, then

$$\frac{d}{dx}[f(x) - g(x)] = \frac{d}{dx}[f(x)] - \frac{d}{dx}[g(x)]$$

Formula 8:(Product Rule) If f and g are both differentiable, then

$$\frac{d}{dx}[f(x)g(x)] = f(x)\frac{d}{dx}(g(x)) + g(x)\frac{d}{dx}(f(x))$$

Formula 9:(Quotient Rule) If f and g are differentiable, then

$$\frac{d}{dx} \left[\frac{f(x)}{g(x)} \right] = \frac{g(x) \frac{d}{dx}(f(x)) - f(x) \frac{d}{dx}(g(x))}{(g(x))^2}$$

Theorem

If $f(x) = \sin(x)$, then $f'(x) = \cos(x)$.

Theorem

If $f(x) = \sin(x)$, then $f'(x) = \cos(x)$.

This is challenging to prove, so we need some lemmas.

Theorem

If $f(x) = \sin(x)$, then $f'(x) = \cos(x)$.

This is challenging to prove, so we need some lemmas.

Lemma

$$\lim_{\theta \rightarrow 0} \frac{\sin(\theta)}{\theta} = 1$$

Lemma

$$\lim_{\theta \rightarrow 0} \frac{(\cos(\theta) - 1)}{\theta} = 0$$