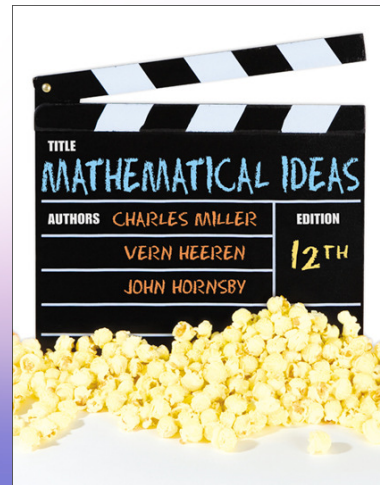


Chapter 2

The Basic Concepts of Set Theory



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Chapter 2: The Basic Concepts of Set Theory

- 2.1 Symbols and Terminology
- 2.2 Venn Diagrams and Subsets
- 2.3 Set Operations and Cartesian Products
- 2.4 Surveys and Cardinal Numbers

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Section 2-1

Symbols and Terminology

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Symbols and Terminology

- Designating Sets
- Sets of Numbers and Cardinality
- Finite and Infinite Sets
- Equality of Sets

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Designating Sets

A **set** is a collection of objects. The objects belonging to the set are called the **elements**, or **members** of the set.

Sets are designated using:

- 1) *word description*,
- 2) *the listing method*, and
- 3) *set-builder notation*.

Designating Sets

Word description

The set of even counting numbers less than 10

The listing method

{2, 4, 6, 8}

Set-builder notation

{ $x \mid x$ is an even counting number less than 10}

Designating Sets

Sets are commonly given names (capital letters).

$$A = \{1, 2, 3, 4\}$$

The set containing no elements is called the **empty set** (*null set*) and denoted by $\{ \}$ or \emptyset .

To show 2 is an element of set A use the symbol \in .

$$2 \in \{1, 2, 3, 4\}$$

$$a \notin \{1, 2, 3, 4\}$$

Example: Listing Elements of Sets

Give a complete listing of all of the elements of the set $\{x \mid x \text{ is a natural number between } 3 \text{ and } 8\}$

Solution

$$\{4, 5, 6, 7\}$$

Sets of Numbers

Natural (*counting*) $\{1, 2, 3, 4, \dots\}$

Whole numbers $\{0, 1, 2, 3, 4, \dots\}$

Integers $\{\dots, -3, -2, -1, 0, 1, 2, 3, \dots\}$

Rational numbers $\left\{ \frac{p}{q} \mid p \text{ and } q \text{ are integers, with } q \neq 0 \right\}$

May be written as a terminating decimal, like 0.25, or a repeating decimal like 0.333...

Irrational $\{x \mid x \text{ is not expressible as a quotient of integers}\}$

Decimal representations never terminate and never repeat.

Real numbers $\{x \mid x \text{ can be expressed as a decimal}\}$

Cardinality

The number of elements in a set is called the **cardinal number**, or **cardinality** of the set.

The symbol $n(A)$, read “ n of A ,” represents the cardinal number of set A .

Example: Cardinality

Find the cardinal number of each set.

- a) $K = \{a, l, g, e, b, r\}$
- b) $M = \{2\}$
- c) \emptyset

Solution

- a) $n(K) = 6$
- b) $n(M) = 1$
- c) $n(\emptyset) = 0$

Finite and Infinite Sets

If the cardinal number of a set is a particular whole number, we call that set a **finite set**.

Whenever a set is so large that its cardinal number is not found among the whole numbers, we call that set an **infinite set**.

Example: Infinite Set

The odd counting numbers are an infinite set.

Word description

The set of all odd counting numbers

Listing method

$\{1, 3, 5, 7, 9, \dots\}$

Set-builder notation

$\{x \mid x \text{ is an odd counting number}\}$

Equality of Sets

Set A is **equal** to set B provided the following two conditions are met:

1. Every element of A is an element of B , and
2. Every element of B is an element of A .

Example: Equality of Sets

State whether the sets in each pair are equal.

- a) $\{a, b, c, d\}$ and $\{a, c, d, b\}$
- b) $\{2, 4, 6\}$ and $\{x \mid x \text{ is an even number}\}$

Solution

- a) Yes, order of elements does not matter
- b) No, $\{2, 4, 6\}$ does not represent all the even numbers.