## Unit 3: Derivatives

## Vocabulary and notation

$$\begin{aligned} f'(x) & \frac{df}{dx}(a) & \frac{d}{dx}\left( \begin{array}{c} \cdots \end{array} \right) \Big|_{x=a} & \text{difference quotient} \\ f''(x) & \frac{d^2f}{dx^2} & \text{differentiable} & \text{one-sided differentiable} \end{aligned}$$

linear operator marginal effect second derivative point of inflection secant line

## Skills

- Write a derivative as a limit
- Capture word problem information involving derivatives
- Graph the derivative of a function whose graph you are given
- Estimate a derivative from a partial lookup table
- Logical implications between differentiability and continuity
- Compute derivatives from first principles for simple cases: constant, linear,  $f(x) := x^2$ .
- Units of the derivative
- Use information about f and its first two derivatives to sketch its graph
- Relation between second derivative, concavity and points of inflection
- Equation for a tangent line in terms of the derivative