## Unit 3: Derivatives

## Vocabulary and notation

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\begin{array}{llll}
f^{\prime}(x) & \frac{d f}{d x}(a) & \left.\frac{d}{d x}(\cdots)\right|_{x=a} & \text { difference quotient } \\
f^{\prime \prime}(x) & \frac{d^{2} f}{d x^{2}} & \text { differentiable } & \text { one-sided differentiable } \\
\text { linear operator } & \text { marginal effect } & \text { second derivative } & \text { point of inflection } \\
\text { secant line } & & &
\end{array}
$$

## Skills

- Write a derivative as a limit
- Capture word problem information involving derivatives
- Graph the derivative of a function whose graph you are given
- Estimate a derivative from a partial lookup table
- Logical implications between differentiability and continuity
- Compute derivatives from first principles for simple cases: constant, linear, $f(x):=x^{2}$.
- Units of the derivative
- Use information about $f$ and its first two derivatives to sketch its graph
- Relation between second derivative, concavity and points of inflection
- Equation for a tangent line in terms of the derivative

