

Diagonalize the matrix

$$L = \begin{bmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix}.$$

1) The characteristic polynomial is  $f_A(\lambda) =$

2) The eigenvalues are:

5) The eigenvectors are

$$\begin{bmatrix} \cdot \\ \cdot \\ \cdot \end{bmatrix} \begin{bmatrix} \cdot \\ \cdot \\ \cdot \end{bmatrix} \begin{bmatrix} \cdot \\ \cdot \\ \cdot \end{bmatrix}$$

5) If  $S$  is the matrix which contains these eigenvectors as columns, then  $S^{-1}AS = D$  is diagonal. This diagonalization is called the **discrete Fourier transform**.

$$S^{-1}AS = \begin{bmatrix} \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot \end{bmatrix}$$