

Homework 2, bonus problem:

Let n and p be positive integers. Prove (combinatorially) that

$$\sum_{i=0}^n \binom{n}{i}^2 p^i = \sum_{j=0}^n \binom{n}{j} \binom{2n-j}{n} (p-1)^j.$$