

```

> restart:
> with(linalg):
Warning, the protected names norm and trace have been redefined and
unprotected
> P:= [[-2,4],[-1,1.1],[0,-0.5],[1,1.0],[2,4.3],[3,8.1]];
      P := [[-2, 4], [-1, 1.1], [0, -0.5], [1, 1.0], [2, 4.3], [3, 8.1]]

```

Let's start off by trying a line

These matrices will solve for the linear (ax + b)

```

> A2:=matrix([[ -2,1],[ -1,1],[ 0,1],[ 1,1],[ 2,1],[ 3,1]]):
B2:=transpose(A2): V2:=matrix([[a],[b]]):
W2:=matrix([[4],[1.1],[-0.5],[1.0],[4.3],[8.1]]):
> evalm(A2)*evalm(V2)=evalm(W2);

```

$$\begin{bmatrix} -2 & 1 \\ -1 & 1 \\ 0 & 1 \\ 1 & 1 \\ 2 & 1 \\ 3 & 1 \end{bmatrix} \begin{bmatrix} a \\ b \end{bmatrix} = \begin{bmatrix} 4 \\ 1.1 \\ -0.5 \\ 1.0 \\ 4.3 \\ 8.1 \end{bmatrix}$$

```

> evalm(B2) * evalm(A2) * evalm(V2) = evalm(B2) * evalm(W2);

```

$$\begin{bmatrix} -2 & -1 & 0 & 1 & 2 & 3 \\ 1 & 1 & 1 & 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} -2 & 1 \\ -1 & 1 \\ 0 & 1 \\ 1 & 1 \\ 2 & 1 \\ 3 & 1 \end{bmatrix} \begin{bmatrix} a \\ b \end{bmatrix} = \begin{bmatrix} -2 & -1 & 0 & 1 & 2 & 3 \\ 1 & 1 & 1 & 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} 4 \\ 1.1 \\ -0.5 \\ 1.0 \\ 4.3 \\ 8.1 \end{bmatrix}$$

```

> evalm(B2&*A2)*evalm(V2) = evalm(B2&*W2);

```

$$\begin{bmatrix} 19 & 3 \\ 3 & 6 \end{bmatrix} \begin{bmatrix} a \\ b \end{bmatrix} = \begin{bmatrix} 24.8 \\ 18.0 \end{bmatrix}$$

```

> solve({19*a + 3*b = 24.8, 3*a + 6*b = 18.0},{a,b});

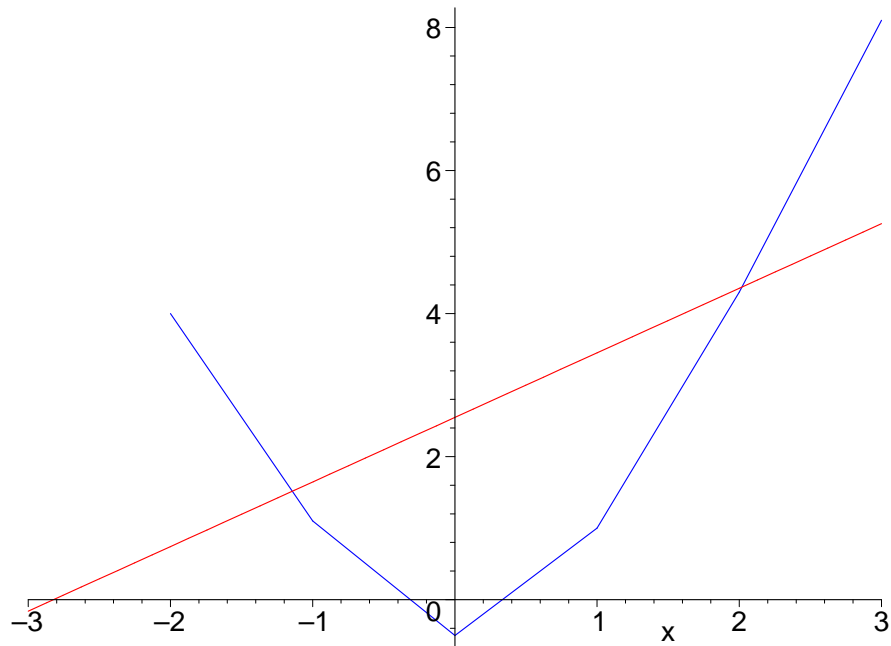
```

$\{a = .9028571429, b = 2.548571429\}$

```

> plot({P,0.9028*x+2.548}, x=-3..3, color=[red, blue]);

```



This doesn't fit too well...let's try a quadratic

These matrices will solve for the quadratic ($ax^2 + bx + c$)

```
> A3:=matrix([[4,-2,1],[1,-1,1],[0,0,1],[1,1,1],[4,2,1],[9,3,1]]);
B3:=transpose(A3); V3:=matrix([[a],[b],[c]]);
W3:=matrix([[4],[1.1],[-0.5],[1.0],[4.3],[8.1]]);
```

```
B3 := transpose(A3)
```

```
> evalm(A3)*evalm(V3)=evalm(W3);
```

$$\begin{bmatrix} 4 & -2 & 1 \\ 1 & -1 & 1 \\ 0 & 0 & 1 \\ 1 & 1 & 1 \\ 4 & 2 & 1 \\ 9 & 3 & 1 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} 4 \\ 1.1 \\ -0.5 \\ 1.0 \\ 4.3 \\ 8.1 \end{bmatrix}$$

```
> evalm(B3) * evalm(A3) * evalm(V3) = evalm(B3) * evalm(W3);
```

$$\begin{bmatrix} 4 & 1 & 0 & 1 & 4 & 9 \\ -2 & -1 & 0 & 1 & 2 & 3 \\ 1 & 1 & 1 & 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} 4 & -2 & 1 \\ 1 & -1 & 1 \\ 0 & 0 & 1 \\ 1 & 1 & 1 \\ 4 & 2 & 1 \\ 9 & 3 & 1 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} 4 & 1 & 0 & 1 & 4 & 9 \\ -2 & -1 & 0 & 1 & 2 & 3 \\ 1 & 1 & 1 & 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} 4 \\ 1.1 \\ -5 \\ 1.0 \\ 4.3 \\ 8.1 \end{bmatrix}$$

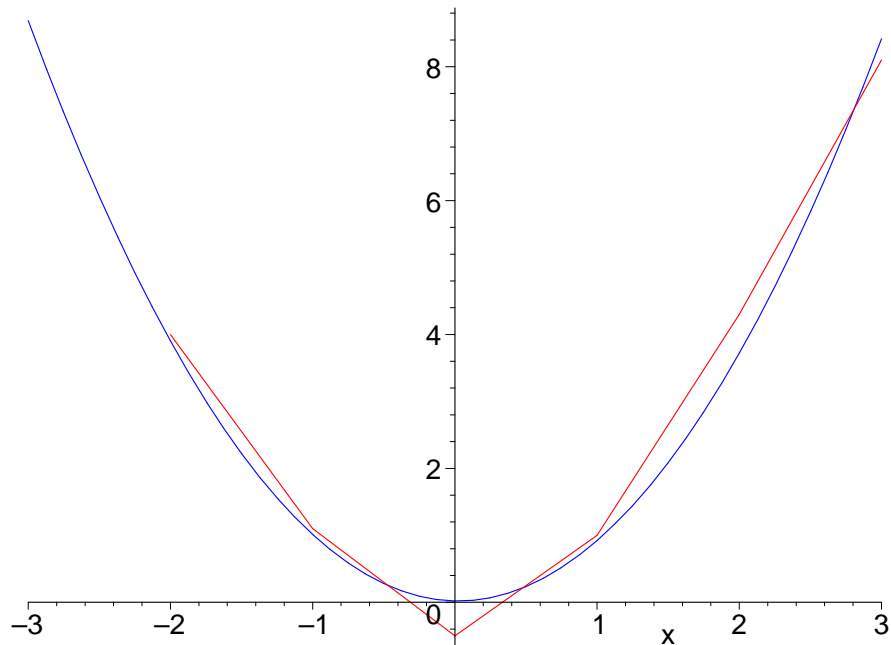
```
> evalm(B3&*A3)*evalm(V3) = evalm(B3&*W3);
```

$$\begin{bmatrix} 115 & 27 & 19 \\ 27 & 19 & 3 \\ 19 & 3 & 6 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} 108.2 \\ 24.8 \\ 18.0 \end{bmatrix}$$

```
> solve({115*a + 27*b + 19*c = 108.2, 27*a + 19*b + 3*c = 24.8, 19*a + 3*b + 6*c = 18.0},{a,b,c});
```

```
      {c=.02000000000, b=-.04535714286, a=.9482142857}
```

```
> plot({P,0.948*x^2 - 0.0454*x + 0.02}, x=-3..3, color=[red,blue]);
```



```
>
```