

1. Assume the acceleration of gravity is 10 m/sec^2 downwards. A cannonball is fired at ground level. If the cannon ball rises to a height of 80 meters and travels a distance of 240 meters before it hits the ground, what is the magnitude of the initial velocity in meters per second?

- (A) 36
- (B) 48
- (C) 50
- (D) 54
- (E) 60
- (F) 64
- (G) 72
- (H) 80
- (I) None of the above

2. Find the equation of the plane that passes through $(1, 3, 2)$ and contains the line

$$\begin{aligned}x &= 1 + t \\y &= -1 - 2t \\z &= 3 + 2t\end{aligned}$$

The y -coordinate of the point where this plane intersects the y -axis is

- (A) -1
- (B) 0
- (C) 1
- (D) 2
- (E) 3
- (F) 4
- (G) 5
- (H) 6
- (I) None of the above

3. Find the curvature for $\mathbf{r}(t) = \langle -t, -\ln(\cos t), 0 \rangle$ at $t = \frac{\pi}{4}$.

- (A) 1
- (B) $\sqrt{2}$
- (C) 2
- (D) $2\sqrt{2}$
- (E) $\frac{\sqrt{2}}{2}$
- (F) $\frac{\sqrt{3}}{2}$
- (G) $3\sqrt{2}$
- (H) $\frac{\sqrt{2}}{3}$
- (I) None of the above

4. Find the arclength of the vector function

$$\mathbf{r}(t) = 3\cos t \mathbf{i} + 3\sin t \mathbf{j} + 2t^{3/2} \mathbf{k}$$

for $0 \leq t \leq 3$.

- (A) 12
- (B) 14
- (C) 16
- (D) 18
- (E) 20
- (F) 24
- (G) 28
- (H) 32
- (I) None of the above

5. Let

$$\mathbf{r}(t) = \sqrt{2} \cos t \mathbf{i} + \sqrt{2} \sin t \mathbf{j} + t \mathbf{k}$$

Using the parametric equations for the line tangent to the function at $t = \frac{\pi}{4}$, find the coordinates of the point where the tangent line intersects the xy -plane.

- (A) $(1, 1, 0)$
- (B) $(1, -1, 0)$
- (C) $\left(1 - \frac{\pi}{4}, 1 + \frac{\pi}{4}, 0\right)$
- (D) $\left(1 + \frac{\pi}{4}, 1 - \frac{\pi}{4}, 0\right)$
- (E) $\left(\frac{\pi}{2} - 1, \frac{\pi}{2} + 1, 0\right)$
- (F) $\left(1, 1, \frac{\pi}{4}\right)$
- (G) $(0, 0, 0)$
- (H) The line does not intersect the xy -plane.
- (I) None of the above

6. Let $z = x\sqrt{y} + \sqrt{x}$ and $x = 2s + t$, $y = s^2 - 7t$. Find $\frac{\partial z}{\partial t}$ when $s = 4$ and $t = 1$.

- (A) $\frac{-22}{3}$
- (B) -7
- (C) -8
- (D) $\frac{-20}{3}$
- (E) $\frac{-23}{3}$
- (F) $\frac{-25}{3}$
- (G) -9
- (H) $\frac{-31}{3}$
- (I) None of the above

7. Let

$$f(x, y, z) = \ln(x^2 + y^2) - z^3.$$

Using the linearization of f at $(-1, 1, 1)$, estimate the value of $f(-0.9, 1.2, 1.1)$.

- (A) 0
- (B) $\ln(2) + 0.7$
- (C) $\ln(2) - 1.2$
- (D) $\ln(2) + 1.3$
- (E) $\ln(2) + 0.5$
- (F) $\ln(2) - 1.6$
- (G) 0.3
- (H) 0.7
- (I) None of the above

8. Let $f(x, y) = x^3 - 3xy + y^2$. Find the local minimum of f .

- (A) $\frac{3}{2}$
- (B) $\frac{5}{2}$
- (C) $\frac{7}{2}$
- (D) $\frac{9}{2}$
- (E) $\frac{25}{16}$
- (F) -2
- (G) $\frac{-27}{16}$
- (H) $\frac{-3}{2}$
- (I) None of the above

9. Find the product of the maximum and minimum values of

$$f(x, y, z) = (x-2)^2 + (y-1)^2 + (z+2)^2 \text{ on the sphere } x^2 + y^2 + z^2 = 1.$$

- (A) 0
- (B) $\sqrt{21}$
- (C) 8
- (D) 16
- (E) 21
- (F) 64
- (G) 80
- (H) 85
- (I) None of the above

10. Compute the integral

$$\int_0^1 \int_0^{2-2x} \frac{(2x-y)^2}{2x+y} dy dx$$

HINT: A change of variable might help

- (A) 0
- (B) $\frac{1}{3}$
- (C) $\frac{4}{9}$
- (D) $\frac{2}{3}$
- (E) $\frac{3}{4}$
- (F) 1
- (G) $\frac{5}{4}$
- (H) $\frac{3}{2}$
- (I) None of the above

11. Find the work done by the force field

$$\mathbf{F} = -\frac{1}{2}x \mathbf{i} - \frac{1}{2}y \mathbf{j} + \frac{1}{4}\mathbf{k}$$

on a particle as it moves along the helix given by

$$\mathbf{r}(t) = \cos t \mathbf{i} + \sin t \mathbf{j} + t \mathbf{k}$$

from the point $(1,0,0)$ to $(-1,0,3\pi)$.

- (A) $\frac{\pi}{4}$ (F) $\frac{\pi}{6}$
 (B) $\frac{\pi}{2}$ (G) $\frac{4\pi}{3}$
 (C) $\frac{3\pi}{2}$ (H) π
 (D) $\frac{3\pi}{4}$ (I) None of the above
 (E) $\frac{\pi}{3}$

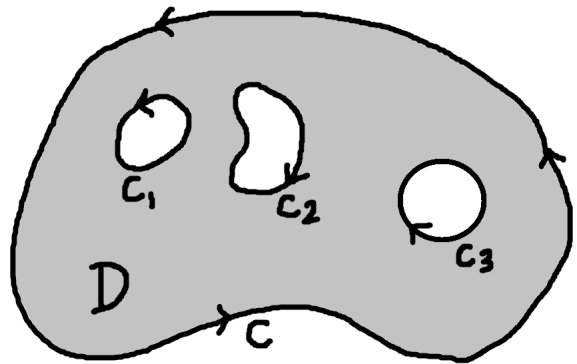
12. Consider the planar region D drawn below whose boundary consists of the curves $C, C_1, C_2,$ and C_3 , oriented as shown. Suppose that $\mathbf{F}(x, y)$ is a vector field whose component functions and their partial derivatives are continuous on D , and that

$$\oint_{C_1} \mathbf{F} \cdot d\mathbf{r} = 1, \quad \oint_{C_2} \mathbf{F} \cdot d\mathbf{r} = -5, \quad \oint_{C_3} \mathbf{F} \cdot d\mathbf{r} = 2, \quad \text{and} \quad \iint_D \left(\frac{\partial Q}{\partial x} - \frac{\partial P}{\partial y} \right) dA = -1.$$

Evaluate

$$\oint_C \mathbf{F} \cdot d\mathbf{r} ?$$

Carefully justify your answer.



- (A) -1
 (B) 0
 (C) 1
 (D) 3
 (E) 5
 (F) -7
 (G) -9
 (H) -11
 (I) None of the above

13. A particle moves along the line segments from $(0,0,0)$ to $(1,0,0)$ to $(1,5,1)$ to $(0,5,1)$ and back to $(0,0,0)$

under the influence of the vector field

$$\mathbf{F}(x, y, z) = z^2\mathbf{i} + 3xy\mathbf{j} + 4y^2\mathbf{k}.$$

Find the work done.

- (A) 0
- (B) 13
- (C) 27
- (D) 30
- (E) $\frac{71}{2}$
- (F) $\frac{73}{2}$
- (G) $\frac{81}{2}$
- (H) $\frac{95}{2}$
- (I) None of the above

14. Let S be the portion of the surface $z = xy$ lying inside the cylinder $x^2 + y^2 = 1$. Compute the surface area S .

- (A) 0
- (B) π
- (C) $\frac{\pi}{2}$
- (D) $\frac{3\pi}{2}$
- (E) $\frac{4\pi}{3}(\sqrt{2}-1)$
- (F) $2\pi(2\sqrt{2}-1)$
- (G) $2\pi(\sqrt{2}-1)$
- (H) $\frac{2\pi}{3}(2\sqrt{2}-1)$
- (I) None of the above

15. A sphere of radius 2 has a hole of radius 1 drilled straight through the center. What is the volume remaining? In terms of inequalities, the region is $R = \{(x, y, z) \mid x^2 + y^2 + z^2 \leq 4 \text{ and } x^2 + y^2 \geq 1\}$.

- (A) 2π
- (B) $4\pi\sqrt{3}$
- (C) 6π
- (D) $4\pi(2 - \sqrt{2})$
- (E) $\frac{4\pi}{9}(12 - \sqrt{3})$
- (F) $10\pi - 2$
- (G) $5\pi\sqrt{3}$
- (H) $4\pi - \sqrt{2}$
- (I) None of the above

16. Let $\mathbf{F}(x, y, z) = z \arctan(y^2) \mathbf{i} + z \ln(x^2 + 3) \mathbf{j} + z \mathbf{k}$.

Find the outward flux of \mathbf{F} through S , the part of the paraboloid $x^2 + y^2 + z = 9$ that lies above the plane $z = 5$ and is oriented upward.

- (A) 0
- (B) 4π
- (C) 6π
- (D) 8π
- (E) 16π
- (F) 24π
- (G) 28π
- (H) 32π
- (I) None of the above

Problem	Answer		Problem	Answer
1	C		9	F
2	G		10	C
3	E		11	D
4	B		12	D
5	D		13	F
6	A		14	H
7	C		15	E
8	G		16	G